

# Average packet delivery delay in intermittently-connected networks

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DIBRIS

University of Genoa, Genoa, Italy

AIRO 2014 - Como, September 2-5, 2014

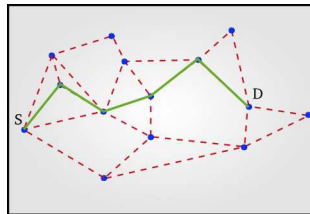
- 1 Intermittently-Connected Networks (ICNs)
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# Intermittently-Connected Networks (ICNs)

## ▶ Intermittently-Connected Networks (ICNs)

### ▶ Characterized by:

- ▶ **intermittent connectivity** (the existence of end-to-end paths between source (S) and destination (D) nodes is not always guaranteed);
- ▶ **long and variable delays**;
- ▶ **asymmetric data rates**;
- ▶ **high error rates**.



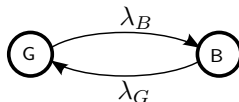
# Networking paradigms for ICNs

- ▶ Two networking paradigms for ICNs.
  - ▶ In the **IP-like paradigm**, incoming packets are stored in routers for a few milliseconds/seconds (**short-term storage**).
    - ▶ In order to transmit the data, the IP-like paradigm requires the availability of a permanently available end-to-end path during the entire transmission.
  - ▶ In the **Delay-Tolerant Networking (DTN) paradigm**, the storage places can hold for a long time messages with no delay constraints (**persistent storage**).
    - ▶ The DTN approach, by adopting a store-and-forward mechanism with longer-term storage, is able to cope with intermittent connectivity and link disruptions.

# Mobility model

- ▶ **Inter-meeting time** and **contact time** between two generic nodes: **exponentially distributed random variables**.
  - ▶ Typical of node mobility models, such Random Waypoint and Random Direction.
- ▶ Behaviour of the communication link between each pair of nodes: described by a **continuous-time Markov chain (CTMC)**.
  - ▶ **Two configurations**.
    - ▶  **$G$  (Good)**: the two nodes are in contact and are able to transmit the data (i.e., **the link is operating**).
    - ▶  **$B$  (Bad)**: the two nodes are not in contact (i.e., the link is disrupted and there is **no connection**. at all).

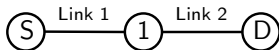
## Model of each communication link



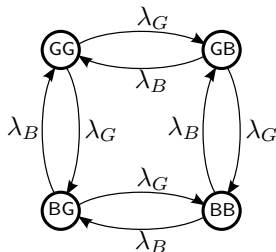
- ▶  $\lambda_G > 0$ : **transition rate** of each link from  $G$  to  $B$ ;
- ▶  $\lambda_B > 0$ : transition rate of each link from  $B$  to  $G$ ;
- ▶  $\tau_G = \frac{1}{\lambda_G}$ : **average lifetime** of the state  $G$ ;
- ▶  $\tau_B = \frac{1}{\lambda_B}$ : average lifetime of the state  $B$ ;
- ▶  $\pi_G = \frac{\tau_G}{\tau_G + \tau_B} = \frac{\lambda_B}{\lambda_G + \lambda_B}$ : **stationary probability** of the state  $G$ ;
- ▶  $\pi_B = \frac{\tau_B}{\tau_G + \tau_B} = \frac{\lambda_G}{\lambda_G + \lambda_B}$ : stationary probability of the state  $B$ .

# Network topology

- ▶  **$L$ -hop network topology**, modeling a **single path source-destination**.
  - ▶  $L$  independent links.
  - ▶ **State of the network** represented by the **ordered  $L$ -tuple of the states** (either  $G$  or  $B$ ) of its links.
- ▶ For  $L = 2$ :



(a) Network topology



(b) The associated CTMC

# Average packet delivery delay

- ▶  $t_{IP}$  and  $t_{DTN}$  : average packet delivery delays experienced by a packet transmitted under the IP-like and DTN paradigms, resp.
  - ▶ Packet generation process: Poisson process.
    - ▶ One can use in the analysis the Poisson Arrivals See Time Averages (PASTA) property.
  - ▶ the Sum of the transmission and propagation delays along each link is modeled by a constant  $\Delta \geq 0$ .
    - ▶ The limit case in which  $\Delta = 0$  models the situation in which both are considered negligible delays.



# IP-like versus DTN paradigm

Differences between the two paradigms.

- ▶ In the **IP-like paradigm**, incoming packets are stored in routers for a few milliseconds/seconds (short-term storage).
  - ▶ In order to transmit the data, the IP-like paradigm requires the availability of a permanently available end-to-end path during the entire transmission.
    - ▶ All the  $L$  links have to be in the good state, for a sufficiently long time interval.
- ▶ In the **Delay-Tolerant Networking (DTN) paradigm**, the storage places can hold for a long time messages with no delay constraints (persistent storage).
  - ▶ The DTN approach, by adopting a store-and-forward mechanism with longer-term storage, is able to cope with intermittent connectivity and link disruptions.
    - ▶ Communication can be successful even if at any time there is only one link in the good state, for a much shorter time interval.

# Goals

## In this talk:

comparing the average packet-delivery delays of IP-like and DTN paradigms.

- ▶ M. Cello, G. Gnecco, M. Marchese, M. Sanguineti, “Evaluation of the Average Packet Delivery Delay in Highly-Disruptive Networks: the “IP-like” and DTN protocol cases”, *IEEE Communications Letters*, vol. 18, pp. 519-522, 2014.
- ▶ M. Cello, G. Gnecco, M. Marchese, M. Sanguineti, “Congestion-Aware Forwarding Strategies for Intermittently Connected Networks”, submitted.

This is a preliminary step towards the following goal:

optimizing the trade-off between the average buffer occupancy and the average packet delivery delay.

# Notations

- ▶  $2^L$  states of the CTMC associated with the  $L$ -hop network topology: ordered in **decreasing lexicographical order**, starting from the state 1 in which all the  $L$  links are in the configuration  $G$ , and ending in the state  $2^L$  in which all the  $L$  links are in the configuration  $B$ .
  - ▶ For example, with  $L = 3$  one gets  
 $\{GGG, GGB, GBG, GBB, BGG, BGB, BBG, BBB\}$
- ▶  $\pi_i$ : **stationary probability of the  $i$ -th state of the CTMC**.
  - ▶ By the link-independence assumption,  $\pi_i = \pi_G^{g(i)} \pi_B^{L-g(i)}$ , where  $g(i)$  is the **number of links in the configuration  $G$  for the state  $i$** .

- ▶  $q_{ij}$ : transition rate from the state  $i$  to the state  $j$ .
  - ▶ For each pair of different states  $i$  and  $j$  of the CTMC,  $q_{ij} \neq 0$  if and only if  $i$  and  $j$  differ in the state of one link only. More specifically,  $q_{ij} = \lambda_B$  if that specific link moves from the configuration  $B$  in the state  $i$  to the configuration  $G$  in the state  $j$ , otherwise  $q_{ij} = \lambda_G$ .
  - ▶ For  $i = j$ , we set (by definition)

$$q_{ii} := - \sum_{l \in \{1, \dots, 2^L\} \setminus \{i\}} q_{il}.$$

- ▶ Expected first hitting time  $k_i$  of the state 1 in which all the links are in the configuration  $G$ : expectation of the first time at which the CTMC, starting from the state  $i$ , “hits” or visits the state 1.
  - ▶ Vector of  $k_i$ 's: minimal non-negative solution of the linear system

$$\begin{cases} k_i = 0, & \text{for } i = 1, \\ -\sum_{j=1}^{2^L} q_{ij} k_j = 1, & \text{for } i = 2, \dots, 2^L \end{cases}$$

- ▶ Simplifications, thanks to symmetry arguments.

# Average packet delivery delay for the IP-like paradigm

## Proposition

Given an  $L$ -hop network topology whose independent links have the same values of  $\lambda_G$  and  $\lambda_B$  and a constant value  $\Delta$  for the sum of transmission and propagation delays, the average packet delivery delay in the IP-like scenario is given by

$$t_{IP} = L\Delta + \frac{1 - p(L\lambda_G, L\Delta)}{p(L\lambda_G, L\Delta)} (\tau(L\lambda_G, L\Delta) + k_{2^L-1}) + \sum_{j=1}^{2^L} \pi_j k_j, \quad (1)$$

where  $p(L\lambda_G, L\Delta) := \int_{L\Delta}^{\infty} (L\lambda_G) e^{-(L\lambda_G)x} dx$  and  $\tau(L\lambda_G, L\Delta) := \int_0^{L\Delta} x \frac{(L\lambda_G) e^{-(L\lambda_G)x}}{1 - e^{-(L\lambda_G)(L\Delta)}} dx$ . For  $L\Delta \simeq 0$ , (1) simplifies to

$$t_{IP} \simeq \sum_{j=1}^{2^L} \pi_j k_j \quad (2)$$

# Average packet delivery delay for the DTN paradigm

## Proposition

Given an  $L$ -hop network topology whose independent links have the same values of  $\lambda_G$  and  $\lambda_B$  and a constant value  $\Delta$  for the sum of the transmission and propagation delays, the average packet delivery delay in the DTN scenario is given by

$$t_{DTN} = L \left[ \Delta + \frac{1 - p(\lambda_G, \Delta)}{p(\lambda_G, \Delta)} (\tau(\lambda_G, \Delta) + \tau_B) + \pi_B \tau_B \right], \quad (3)$$

where  $p(\lambda_G, \Delta) := \int_{\Delta}^{\infty} \lambda_G e^{-\lambda_G x} dx$  and  $\tau(\lambda_G, \Delta) := \int_0^{\Delta} x \frac{\lambda_G e^{-\lambda_G x}}{1 - e^{-\lambda_G \Delta}} dx$ . For  $\Delta \simeq 0$ , (3) simplifies to

$$t_{DTN} \simeq L \pi_B \tau_B \quad (4)$$

# Comparison of the two approaches

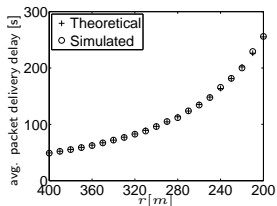
- ▶ Comparison of the performances of the IP-like and DTN approaches carried out
  - ▶ both **numerically**, via formulas (1) and (3) provided by Propositions 1 and 2, resp.,
  - ▶ and **by using an event-driven ad-hoc simulator written in C++**,under various levels of network disruption.



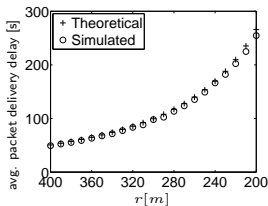
## Scenarios

- ▶ **Random Waypoint mobility model** on a square of size  $1km^2$  with speed chosen uniformly in  $[14.5, 36]m/s$ .
- ▶ **Transmission radius  $r$  of the nodes** (i.e., the largest inter-node distance under which the associated link is in the configuration  $G$ ): from  $400m$  to  $200m$ .
  - ▶ Associated values of  $\lambda_G$ : from  $0.0478s^{-1}$  to  $0.0955s^{-1}$ .
  - ▶ Associated values of  $\lambda_B$ : from  $0.0328s^{-1}$  to  $0.0164s^{-1}$ .
- ▶ We have varied also the number  $L$  of hops and the value  $\Delta$  of the sum of the transmission and propagation delays.

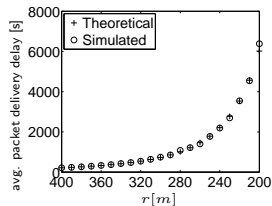
# Results for the IP-like paradigm



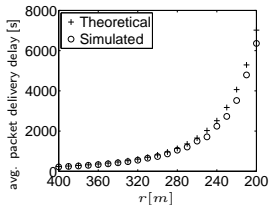
(c)  $L = 2, \Delta = 0$  s



(d)  $L = 2, \Delta = 0.1$  s

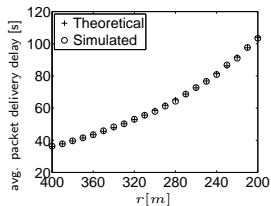


(e)  $L = 4, \Delta = 0$  s

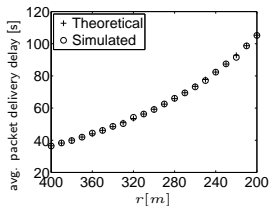


(f)  $L = 4, \Delta = 0.1$  s

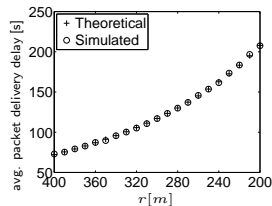
# Results for the DTN paradigm



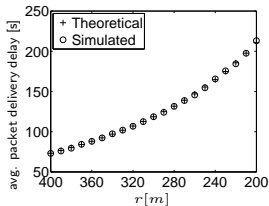
(g)  $L = 2, \Delta = 0$  s



(h)  $L = 2, \Delta = 0.1$  s



(i)  $L = 4, \Delta = 0$  s



(j)  $L = 4, \Delta = 0.1$  s

## Comments

- ▶ For an increasing number  $L$  of hops and a decreasing value of the transmission radius  $r$ , in the considered ICN scenarios the DTN approach dramatically outperforms the IP-like one.
- ▶ In most cases, the simulated curves are practically overlapped to the theoretical ones.
  - ▶ This is due to the ergodicity of the underlying continuous-time Markov chain of the two models.
  - ▶ The maximum relative error in the results presented is referred to the IP-like case for  $L = 2$ ,  $\Delta = 0.1s$  and  $r = 200m$ , and is below 6.5%.
- ▶ The results confirm and address quantitatively the fact (realized experimentally in various works) that, when the network experiences a high degree of disruption, DTN outperforms the IP-like paradigm in terms of a smaller average packet delivery delay.

# Extensions

- ▶ We have focused on the case of an  $L$ -hop network topology modeling a single source-destination path.
- ▶ Possible extensions of the model to the case of multiple paths (e.g., nodes organized in layers).
- ▶ Simplest extension to the case of a more complex topology and multiple paths: interpreting  $L$  - for the DTN paradigm - as the average number of hops in the first path that delivers the packet to the destination.
  - ▶ In this case,  $L$  being the same, the comparison is still in favour of DTN. The model overestimates  $t_{DTN}$ , since the path under consideration is not generic, but the one that minimizes the packet delivery delay with respect to several paths.

- ▶ Investigating the dependencies of the obtained expressions  $t_{IP}$  and  $t_{DTN}$  on their parameters  $(L, \lambda_G, \lambda_B, \Delta)$ .
- ▶ Evaluating and optimizing the trade-off between the average buffer occupancy and the average packet delivery delay.
  - ▶ DTN paradigm: larger average buffer occupancy, smaller average packet delivery delay.
  - ▶ IP-like paradigm: smaller average buffer occupancy, larger average packet delivery delay.
- ▶ Case of many source/destination pairs: possible analysis through noncooperative game theory.
  - ▶ Congestion avoidance through transmission rate adaptation.

Thank you for your attention

## References

1. M. Cello, G. Gnecco, M. Marchese, M. Sanguineti, “Evaluation of the Average Packet Delivery Delay in Highly-Disruptive Networks: the “IP-like” and DTN protocol cases”, *IEEE Communications Letters*, vol. 18, pp. 519-522, 2014.
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